

certain defination :-

① Kinetic energy of the body is given by

$$T = \frac{1}{2} m v^2$$

② Potential energy of the body is given by the force to displace the body against any internal force.

Gravitational potential energy.

$$V = mgh$$

Elastic Potential energy

$$V = \frac{1}{2} k x^2$$

where  $k = \frac{F}{\Delta l}$  = spring constant

③ Pressure energy  $E_p = \text{Pressure} \times \text{change in volume}$ .

$$E_p = P \cdot dV$$

④ Lagrangian function :- The difference of K.E and Potential energy is k/a Lagrangian function  $L$

$$L = T - V$$

⑤ Hamilton function :- The sum of K.E and PE is k/a Hamilton function  $H = T + V$

classical Mechanics is divided into three Groups

- (1) Newtonian Mechanics
- (2) Lagrangian Mechanics
- (3) Hamiltonian Mechanics

Newtonian motion deal the force, displacement, acceleration, work, Power, energy of body or system  
Lagrangian Mechanics deals the motion of the body with the difference of K.E & P.E

$$L = T - V$$

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Hamiltonian mechanics deals the motion of the particle or system in terms of sum of K.E & P.E

$$H = T + V$$

## Newtonian Mechanics

Frame of reference: - The co-ordinate axis attached to the body and observer is k/a frame of reference.

Inertial frame of reference: - The frame of reference which obey the law of inertia is k/a inertial frame of reference.

Hence, body is in uniform motion or at rest has inertial frame of reference.

Let us consider the inertial frame of reference  $S$  and  $S'$  in which  $S$  is at rest and  $S'$  is moving with uniform velocity  $v$  along  $x$ -axis.

The transformation is given by (co-ordinate)

$$x = x' + vt$$

Differentiating it,

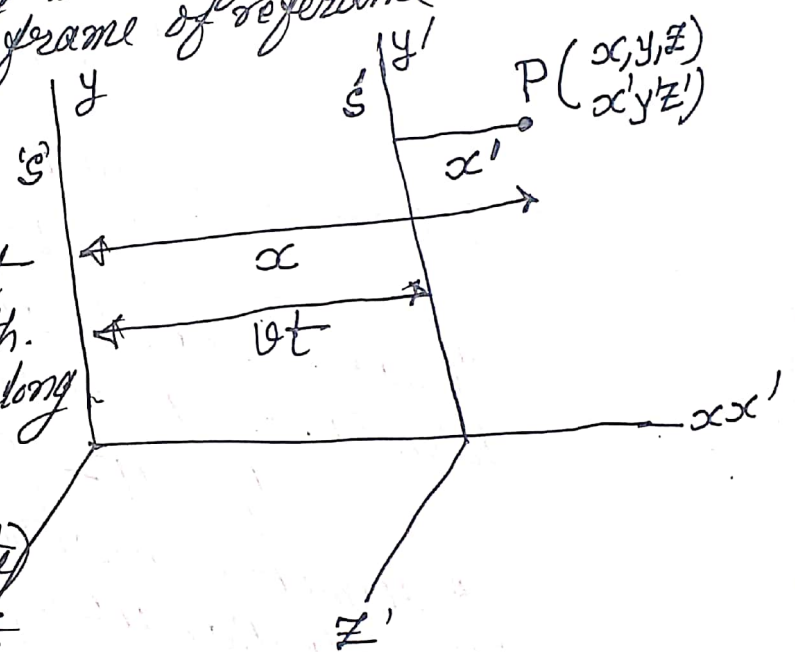
$$\frac{dx}{dt} = \frac{dx'}{dt} + v$$

$$u = u' + v \quad \text{--- (A)}$$

Where  $u$  and  $u'$  are the velocity of Particle  $P$  in  $S$  and  $S'$  frame respectively.

Differentiating eqn (A) again

$$\frac{du}{dt} = \frac{du'}{dt} + 0 \Rightarrow a = a'$$





If  $m =$  mass of the Particle  $P$ . then

$$ma = ma'$$

$$\text{or, } \boxed{F = F'}$$

Hence, the force acting upon the particle in both frame are same, Hence, the law of Physics are same in inertial frame.

Non-inertial frame of reference or accelerated frame of reference:-

The frame of reference attached to the accelerated body is k/a non-inertial frame of reference.

Let the body moving with uniform velocity  $v$  for the time  $t$ . The transformation co-ordinate is given by

$$\boxed{x = x' + vt}$$

Differentiating it we get  $\neq$

$$\frac{dx}{dt} = \frac{dx'}{dt} + v \text{ or, } u = u' + v$$

If the body accelerated after the time  $t$  then.

$$\frac{du}{dt} = \frac{du'}{dt} + \frac{dv}{dt}$$

$$\text{or, } a = a' + a''$$

Where  $a$  and  $a'$  are the acceleration of the body with respect to  $S$  and  $S'$ . The force acting upon the particle is given by

$$ma = ma' + ma''$$

$$F = F' + F''$$

Hence, in the accelerated frame a vertical force  $F''$  is developed k/a Pseudoforce.

